## UNISEX LIFE EXPECTANCIES AT BIRTH AND AGE 65

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Life expectancies at birth and age 65 are shown in tables V.A3 and V.A4 of the 2004 Annual Report of the Board of Trustees. The life expectancies in those tables are presented on both a period and a cohort basis, separately, for males and females. This note provides the corresponding unisex life expectancies, and a brief explanation of their calculation method.

The following standard actuarial functions<sup>1</sup> are used in this note:

 $\mathring{e}_x$  = the average number of years of life remaining at exact age x

 $l_x$  = the number of persons surviving to exact age x

 $l_0$  = the starting number of persons in life table at age 0 (radix)

Additionally, a second subscript is used to denote gender where the letters u, m, and f represent unisex, male, and female, respectively.

The Office of the Chief Actuary computes all unisex life table values from the corresponding male and female life tables based on the observation that there are approximately 1,050 males born for every 1,000 females each year. <sup>2</sup> Thus, a unisex life table is created by combining a male life table with radix <sup>3</sup> 105,000 and a female life table with radix 100,000, and then rescaling the combined table to radix 100,000. Unisex life expectancy at birth is then 1.05 times male life expectancy at birth plus female life expectancy at birth, this sum divided by 2.05.

$$\mathring{e}_{0,u} = \frac{1.05 \, \mathring{e}_{0,m} + 1.00 \, \mathring{e}_{0,f}}{2.05} \tag{1}$$

At a given age x, the unisex life expectancy may be calculated as<sup>4</sup>

$$\mathring{e}_{x,u} = \frac{l_{x,m} \mathring{e}_{x,m} + l_{x,f} \mathring{e}_{x,f}}{l_{x,m} + l_{x,f}}.$$
 (2)

For the unisex life expectancy at birth, notice that Equation (2) reduces to Equation (1) for the case where x = 0,  $l_{0,m} = 105,000$  and  $l_{0,f} = 100,000$ . For age 65, the unisex life expectancy is computed as<sup>4</sup>

$$\mathring{e}_{65,u} = \frac{l_{65,m} \mathring{e}_{65,m} + l_{65,f} \mathring{e}_{65,f}}{l_{65,m} + l_{65,f}}.$$
 (3)

The tables on the following pages correspond to tables V.A3 and V.A4 of the 2004 Trustees Report. Table 1 presents historical and projected unisex life expectancies on a period basis (for the intermediate alternative, only) in the same format as table V.A3 of the Trustees Report. Similarly, table 2 shows the unisex life expectancies on a cohort basis in the same format as table V.A4 of the Trustees Report. Detailed versions of tables 1 and 2 which contain unisex life expectancies for all years from 1940-2080 are available for internet download. For the purpose of comparison and easy accessibility, gender specific life expectancies are included in tables 1 and 2.

<sup>&</sup>lt;sup>1</sup> These actuarial functions are described in chapter IV of Actuarial Study Number 116, Life Tables for the United States Social Security Area. 1900-2100. www.socialsecurity.gov/OACT/NOTES/as116/as116\_IV.html

<sup>&</sup>lt;sup>2</sup> See the National Vital Statistics Report, Volume 52, Number 10, page 8 for a description of the sex ratio.

 $<sup>^3</sup>$  The radix of a life table is defined as  $l_0$ , and is selected to be an arbitrarily but generally large integer.

 $<sup>^4</sup>$  This equation is based on a male life table radix of 105,000 and a female life table radix of 100,000.

<sup>&</sup>lt;sup>5</sup> www.socialsecurity.gov/OACT/NOTES/an2004-2/index.html

Table 1.—Period Life Expectancies<sup>1</sup>

	Unisex		Male		Female	
Calendar Year	At birth	At age 65	At birth	At age 65	At birth	At age 65
Historical Data:						-
1940	63.5	12.7	61.4	11.9	65.7	13.4
1945	65.6	13.6	62.9	12.6	68.4	14.4
1950	68.3	14.0	65.6	12.8	71.1	15.1
1955	69.7	14.5	66.7	13.1	72.8	15.6
1960	69.9	14.5	66.7	12.9	73.2	15.9
1965	70.2	14.8	66.8	12.9	73.8	16.3
1970	70.9	15.3	67.2	13.1	74.9	17.1
1975	72.6	16.0	68.7	13.7	76.6	18.0
1980	73.6	16.3	69.9	14.0	77.5	18.4
1985	74.6	16.6	71.1	14.4	78.2	18.6
1990	75.2	17.1	71.8	15.0	78.9	19.0
1991	75.4	17.2	72.0	15.1	79.0	19.1
1992	75.6	17.3	72.2	15.2	79.2	19.2
1993	75.4	17.1	72.0	15.1	78.9	19.0
1994	75.6	17.2	72.3	15.3	79.0	19.0
1995	75.7	17.2	72.5	15.3	79.0	19.0
1996	76.0	17.3	72.9	15.4	79.2	19.0
1997	76.3	17.3	73.4	15.5	79.3	19.1
1998	76.4	17.4	73.7	15.6	79.4	19.0
1999	76.5	17.3	73.8	15.7	79.3	18.9
2000	76.6	17.4	74.0	15.8	79.4	18.9
2001 <sup>2</sup>	76.7	17.5	74.1	15.9	79.4	18.9
2002 <sup>2</sup>	76.8	17.5	74.3	16.0	79.5	18.9
2003 <sup>2</sup>	76.9	17.5	74.4	16.0	79.5	19.0
Projected: <sup>3</sup>						
2005	77.1	17.6	74.7	16.1	79.6	19.0
2010	77.6	17.8	75.3	16.4	80.0	19.1
2015	78.0	18.1	75.8	16.7	80.4	19.4
2020	78.5	18.4	76.3	17.1	80.8	19.7
2025	79.0	18.7	76.9	17.4	81.3	20.0
2030	79.5	19.0	77.4	17.7	81.7	20.3
2035	79.9	19.3	77.8	18.0	82.1	20.6
2040	80.4	19.6	78.3	18.2	82.5	20.9
2045	80.8	19.9	78.8	18.5	82.9	21.2
2050	81.2	20.1	79.2	18.8	83.3	21.4
2055	81.6	20.4	79.6	19.1	83.6	21.7
2060	82.0	20.6	80.0	19.3	84.0	22.0
2065	82.3	20.9	80.4	19.6	84.3	22.2
2070	82.7	21.2	80.8	19.9	84.6	22.5
2075	83.0	21.4	81.2	20.1	85.0	22.7
2080	83.4	21.6	81.6	20.3	85.3	22.9

<sup>&</sup>lt;sup>1</sup> The period life expectancy at a given age for a given year represents the average number of years of life remaining if a group of persons at that age were to experience the mortality rates for the year over the course of their remaining lives. <sup>2</sup> Preliminary or estimated.

Actuarial Note No. 2004.2 Social Security Administration Office of the Chief Actuary Baltimore, Maryland September 2004

<sup>&</sup>lt;sup>3</sup> The projected values are based on the intermediate assumptions of the 2004 Trustees Report.

Table 2.—Cohort Life Expectancies<sup>1</sup>

Calendar Year	Unisex		Male		Female	
	At birth <sup>2</sup>	At age 65 <sup>3</sup>	At birth <sup>2</sup>	At age 65 <sup>3</sup>	At birth <sup>2</sup>	At age 65 <sup>3</sup>
1940	72.5	13.8	69.5	12.7	75.8	14.7
1945	74.1	14.3	71.1	13.0	77.3	15.4
1950	75.3	14.7	72.3	13.1	78.5	16.2
1955	76.0	15.1	73.1	13.1	79.1	16.7
1960	76.6	15.5	73.8	13.2	79.6	17.4
1965	77.3	15.9	74.6	13.5	80.2	18.0
1970	78.3	16.4	75.7	13.8	81.0	18.5
1975	79.1	16.7	76.6	14.2	81.7	18.7
1980	79.8	16.9	77.5	14.7	82.3	18.7
1985	80.5	17.1	78.1	15.2	82.9	18.8
1990	81.0	17.4	78.8	15.6	83.4	19.0
1991	81.1	17.4	78.9	15.7	83.5	19.0
1992	81.2	17.5	79.0	15.8	83.6	19.0
1993	81.3	17.6	79.1	15.9	83.6	19.1
1994	81.4	17.6	79.2	16.0	83.7	19.1
1995	81.6	17.7	79.4	16.0	83.9	19.1
1996	81.7	17.7	79.5	16.1	83.9	19.2
1997	81.8	17.8	79.6	16.2	84.0	19.2
1998	81.8	17.9	79.7	16.3	84.1	19.3
1999	81.9	17.9	79.8	16.4	84.2	19.3
2000	82.0	18.0	79.9	16.5	84.3	19.4
2001	82.1	18.1	80.0	16.6	84.3	19.4
2002	82.2	18.1	80.1	16.6	84.4	19.5
2003	82.3	18.2	80.2	16.7	84.5	19.5
2005	82.5	18.3	80.4	16.8	84.7	19.7
2010	82.9	18.6	80.8	17.2	85.0	20.0
2015	83.3	18.9	81.3	17.5	85.4	20.3
2020	83.6	19.2	81.7	17.8	85.7	20.6
2025	84.0	19.5	82.1	18.1	86.0	20.9
2030	84.4	19.8	82.5	18.4	86.4	21.2
2035	84.7	20.1	82.8	18.7	86.7	21.5
2040	85.0	20.4	83.2	19.0	87.0	21.7
2045	85.4	20.6	83.5	19.3	87.3	22.0
2050	85.7	20.9	83.9	19.5	87.6	22.3
2055	86.0	21.2	84.2	19.8	87.8	22.5
2060	86.3	21.4	84.5	20.1	88.1	22.8
2065	86.6	21.7	84.9	20.3	88.4	23.0
2070	86.8	21.9	85.2	20.6	88.6	23.3
2075	87.1	22.1	85.5	20.8	88.9	23.5
2080	87.4	22.4	85.8	21.1	89.1	23.7

<sup>&</sup>lt;sup>1</sup> The cohort life expectancy at a given age for a given year represents the average number of years of life remaining if a group of persons at that age were to experience the mortality rates for the series of years in which they reach each succeeding age. All mortality rates are consistent with those used for the intermediate assumptions of the 2004 Trustees Report.

Actuarial Note No. 2004.2 Social Security Administration Office of the Chief Actuary Baltimore, Maryland September 2004

<sup>&</sup>lt;sup>2</sup> Cohort life expectancies at birth are based on a combination of actual and projected data for birth years prior to 2001. For birth years after

<sup>2000,</sup> these values are based on projected data.

3 Age 65 cohort life expectancies are based on actual data prior to 1970. For 1970 through 2000, these values are based on a combination of actual and projected data. After 2000, these values are based on projected data.